

# Diffraction and Imaging

## part IV

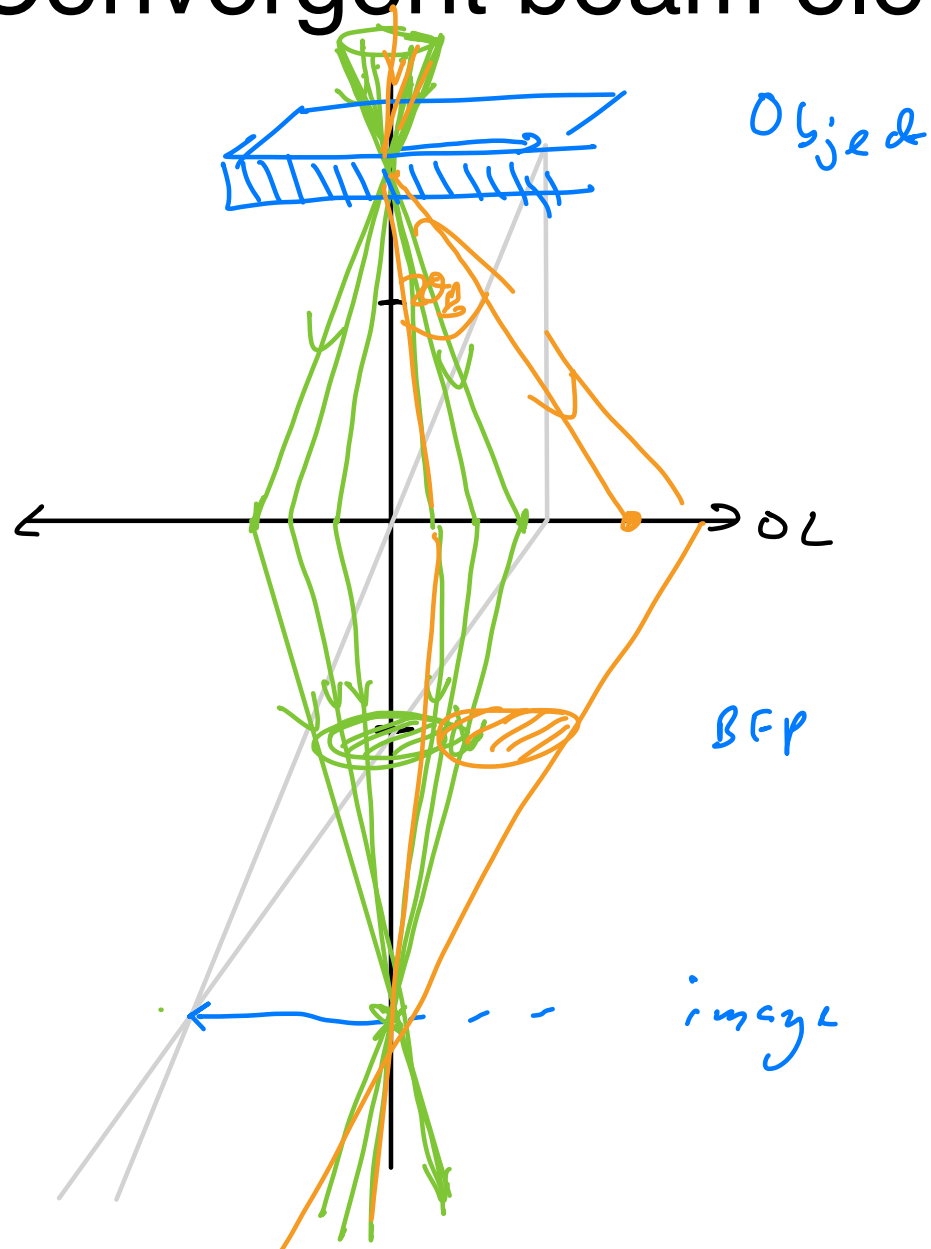
**Duncan Alexander**

EPFL-IPHYS-LSME

# EPFL Diffraction and imaging IV program

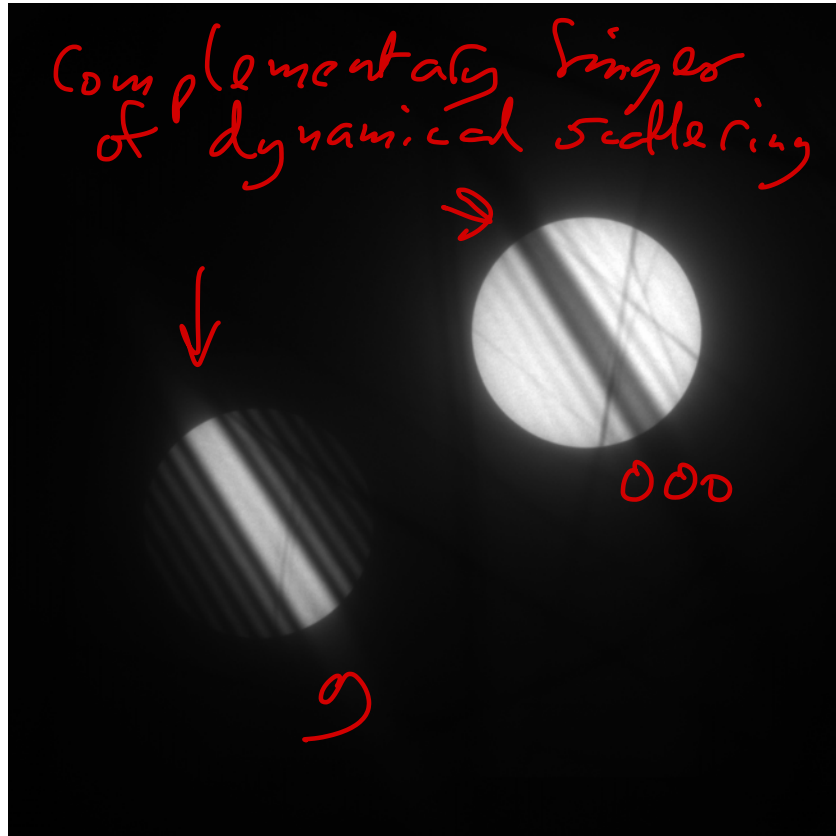
- Q and A from MOOC week 6 lectures and exercises
- Mini-lecture on:
  - Convergent beam electron diffraction (CBED)
- Demos: CBED (2-beam, zone axis) and FOLZ using silicon [0 0 1] sample

Focus  $e^-$   
beam on  
sample

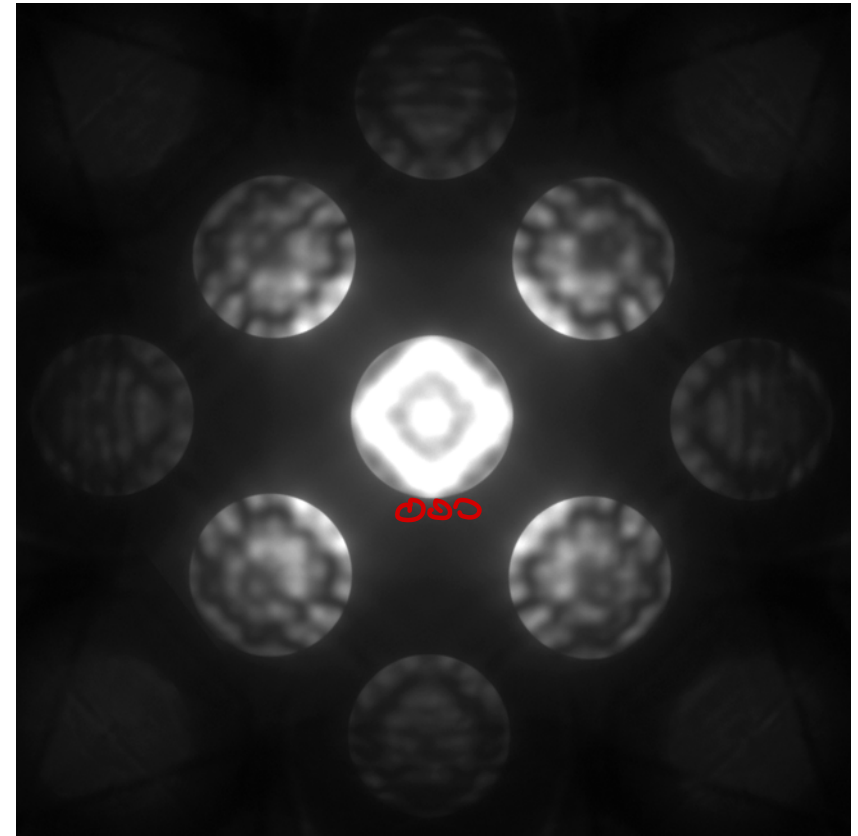


→ Pattern of  
Discs in BFP!

- 2-beam CBED pattern (Si):

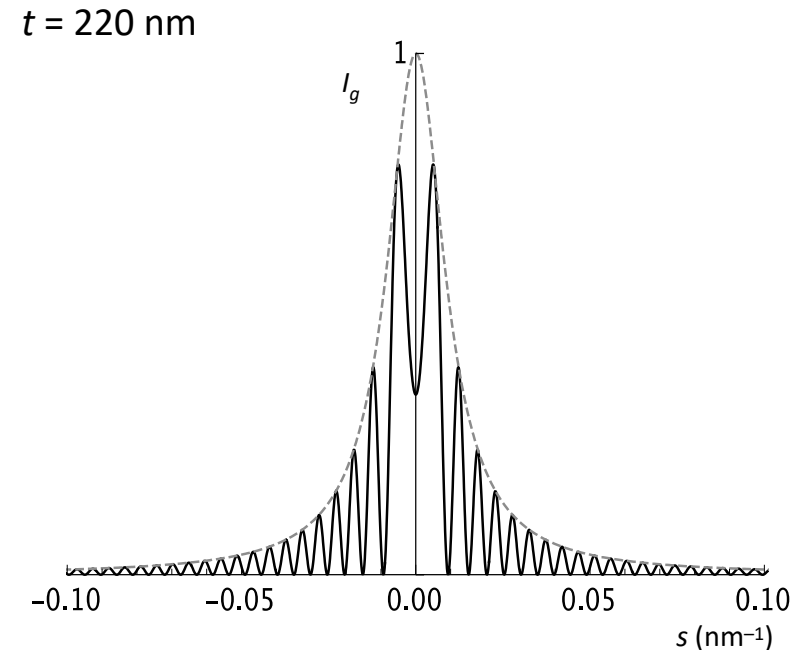
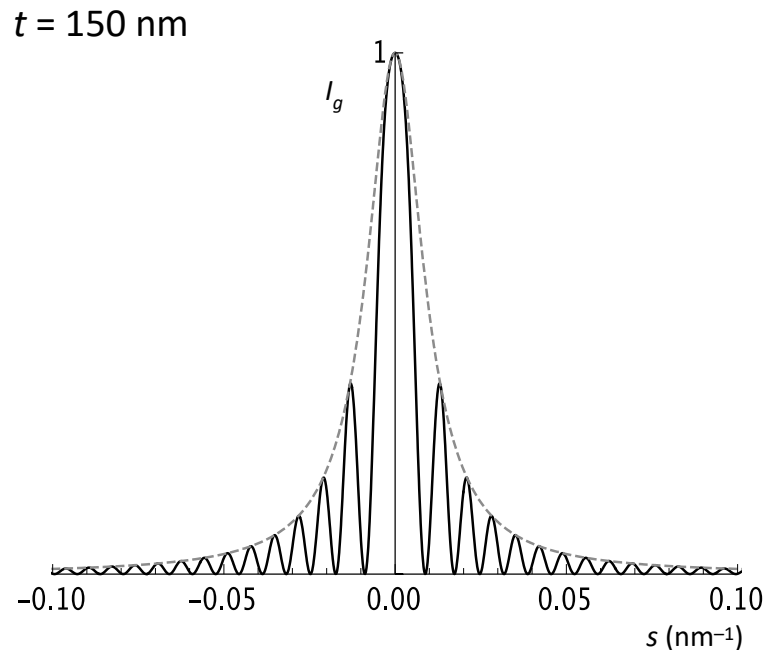


- [0 0 1] zone axis CBED pattern (Si):



# EPFL Recap: Beam intensities in 2-beam condition

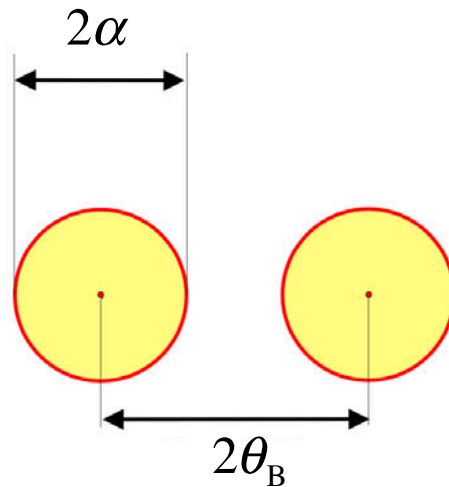
- Intensity in diffracted beam:  $I_g(t) = \frac{1}{1 + \xi_g^2 s^2} \sin^2 \left( \pi t \sqrt{\frac{1}{\xi_g^2} + s^2} \right)$
- Intensity in direct beam:  $I_0(t) = 1 - I_g(t)$
- Model  $I_g$  vs  $s$  for  $\xi_g = 100 \text{ nm}$



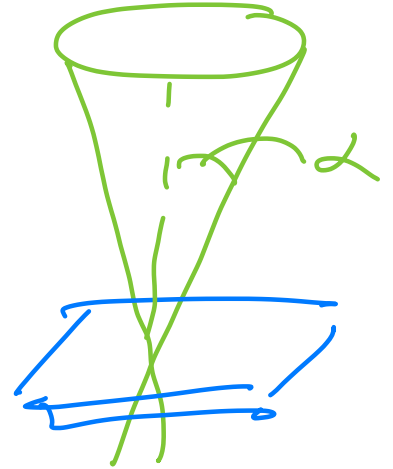
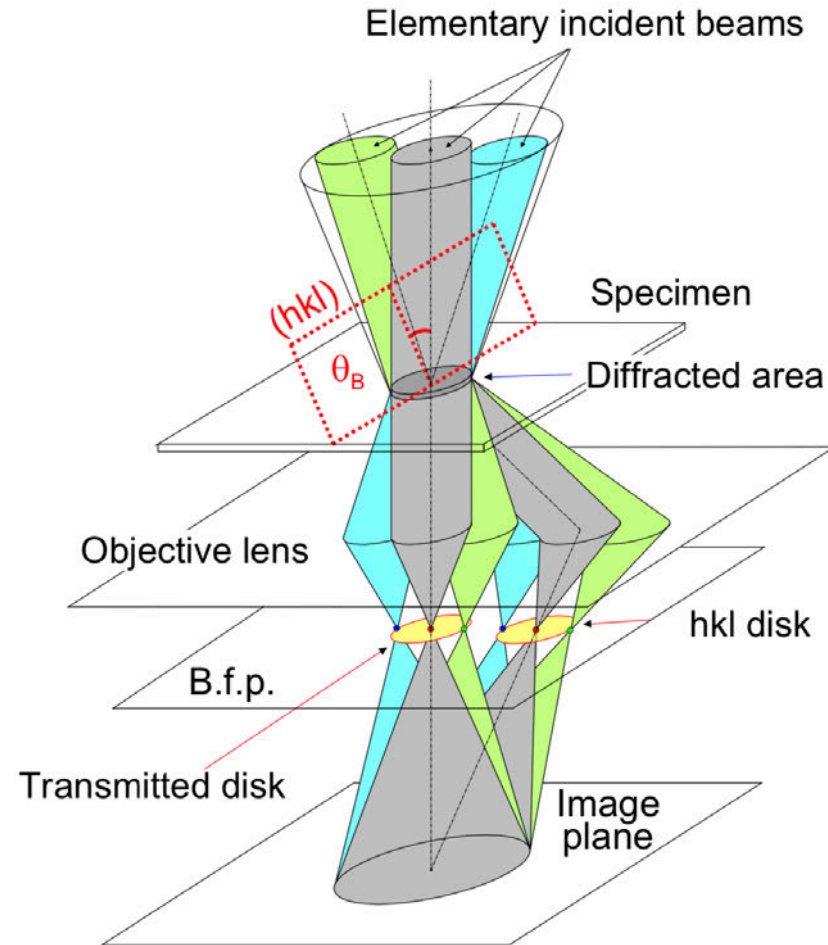
# EPFL CBED 2-beam condition

- 2-beam illustration with semi-focused beam (from J.-P. Morniroli)

Consider convergent beam  
as parallel incident rays at  
different angles

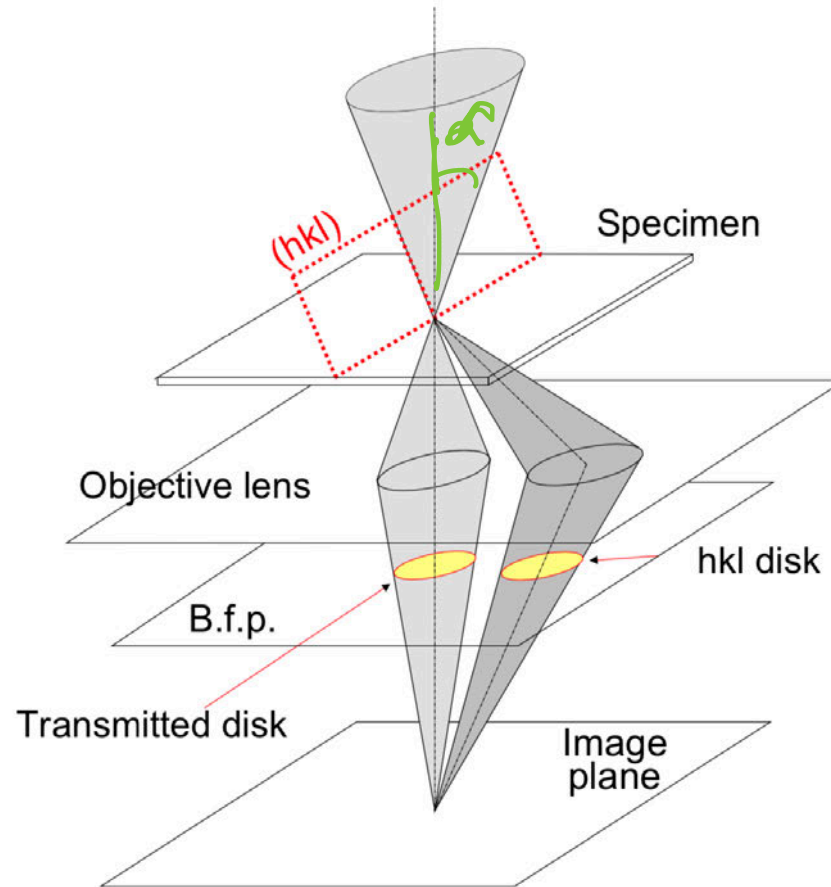
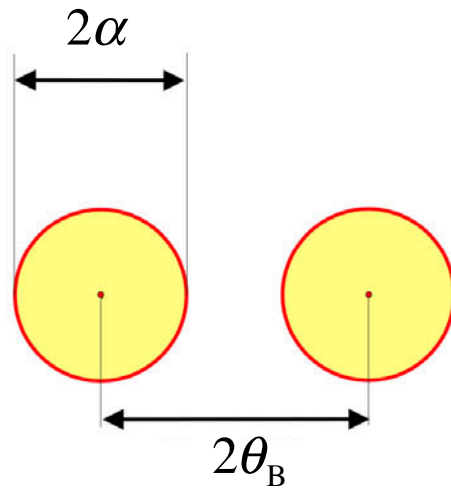


$\alpha$  : convergence  
semi-angle



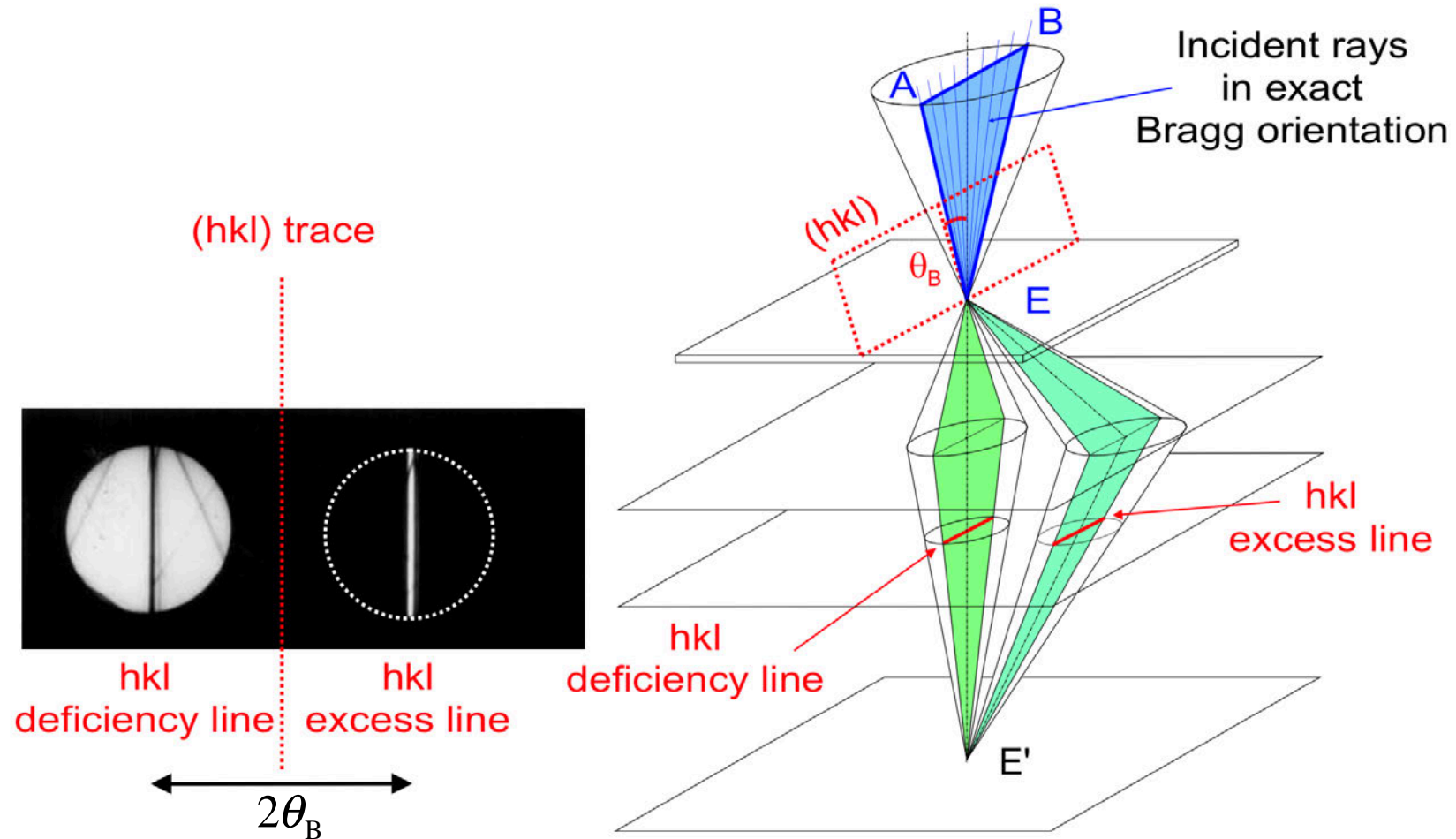
# EPFL CBED 2-beam condition

- 2-beam illustration with fully-focused beam (from J.-P. Morniroli)



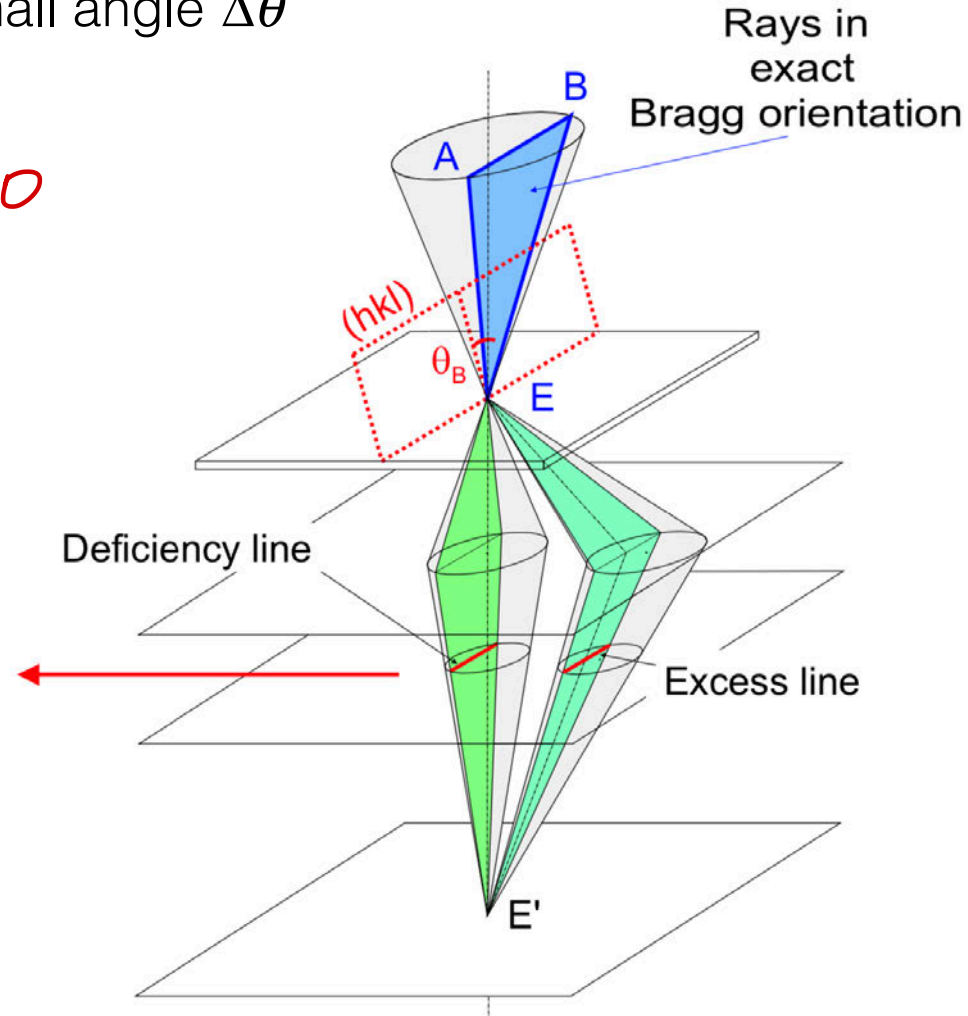
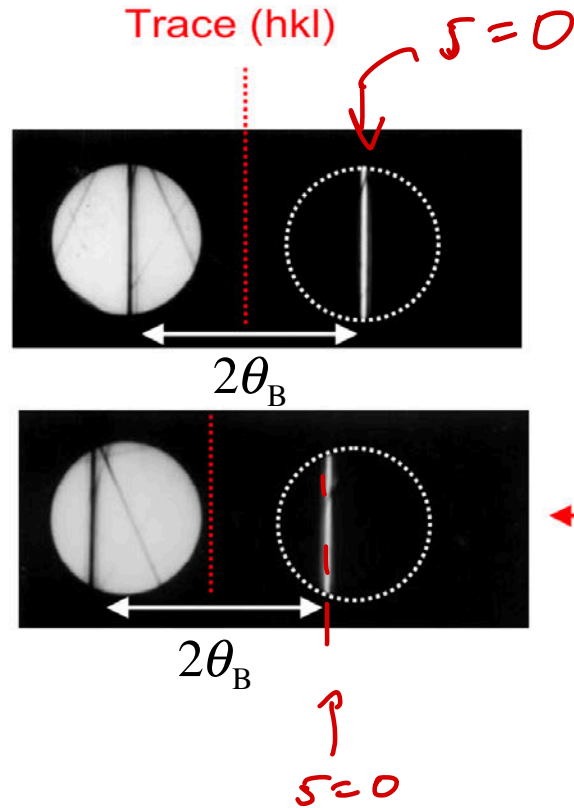
# EPFL CBED 2-beam condition

- 2-beam illustration with fully-focused beam (from J.-P. Morniroli)



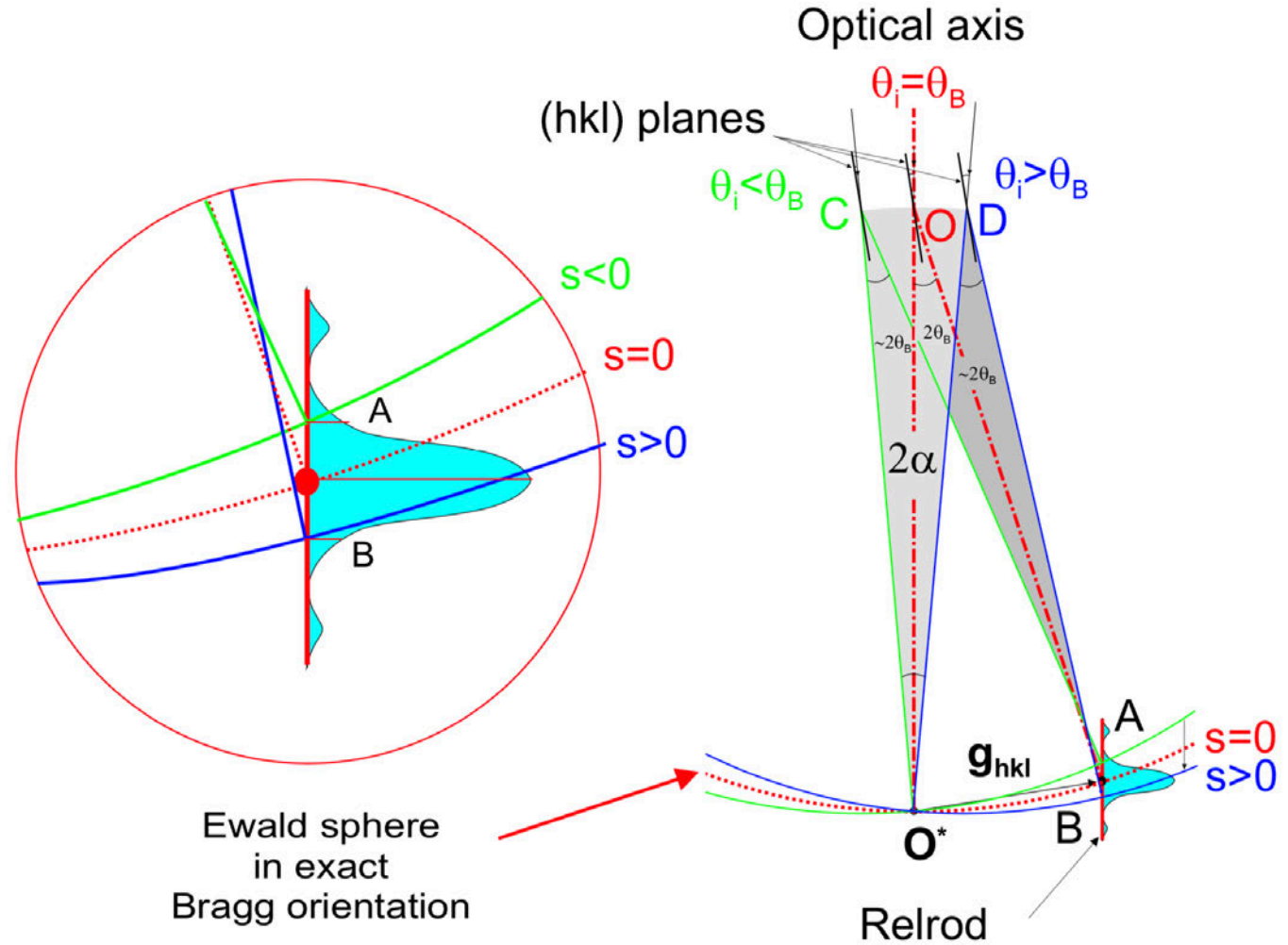


- Tilt Bragg-diffracting plane by small angle  $\Delta\theta$



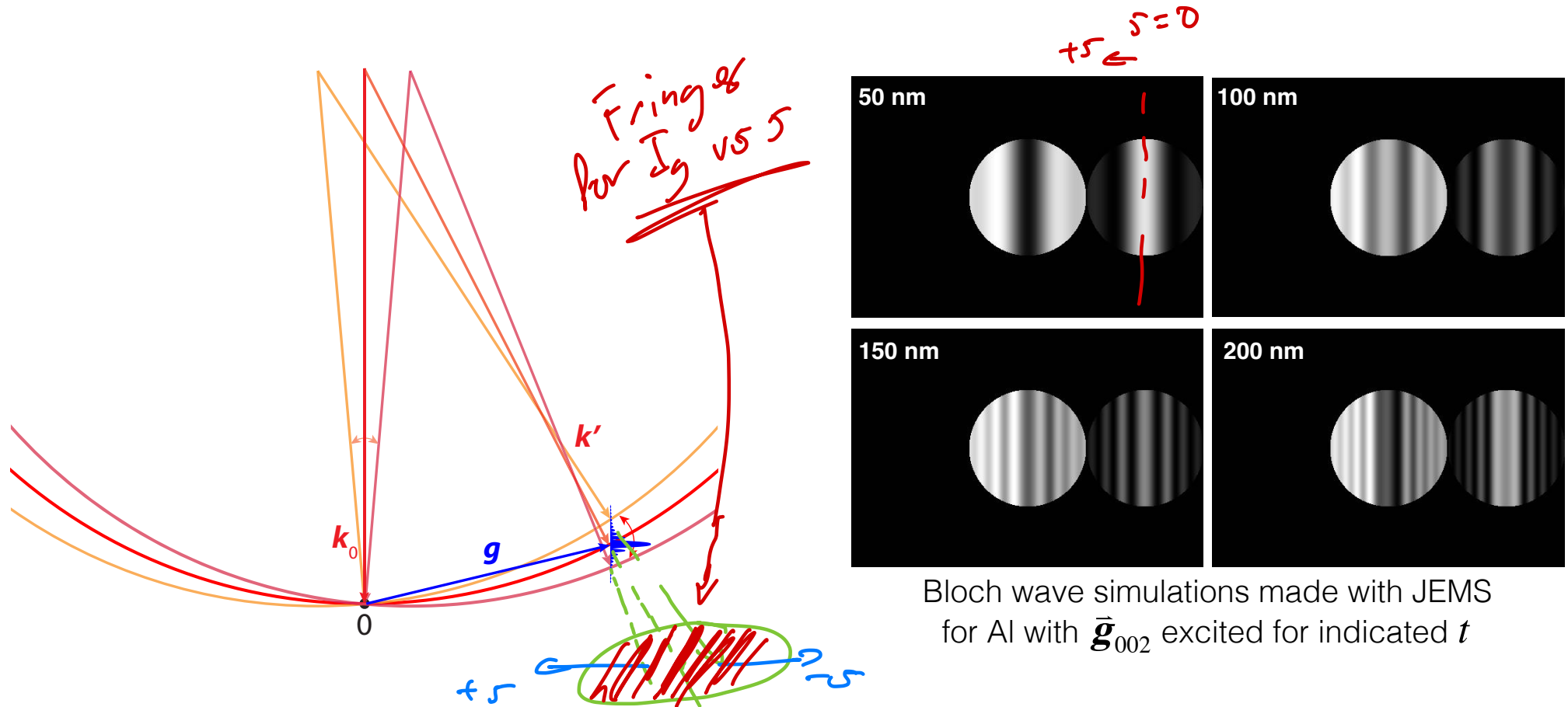
# CBED: measure $I_g$ vs $s$

- $\Rightarrow$  we can measure  $I_g$  vs  $s$  along a chord in the CBED disc for reflection  $g$

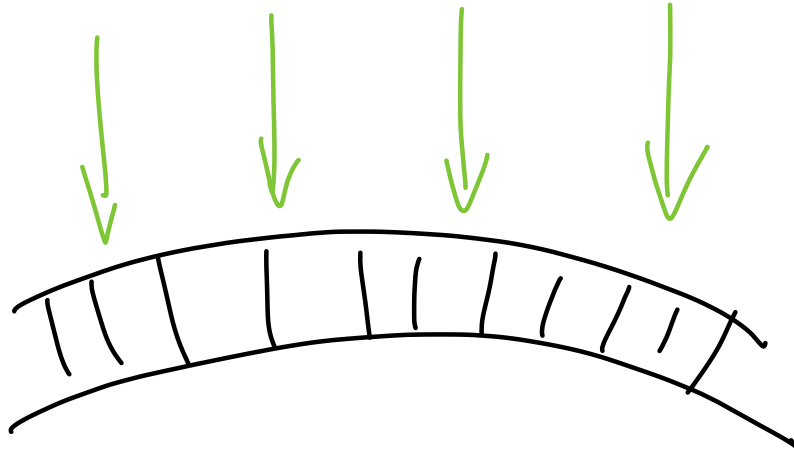


# EPFL CBED: thickness fringes

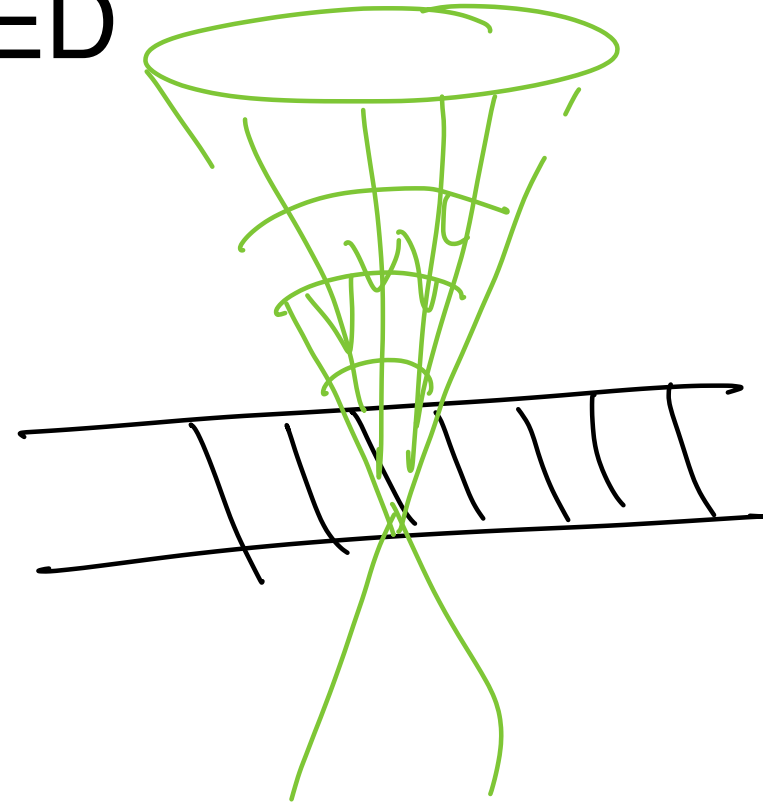
- 2-beam condition: CBED discs with 1-D fringes
- Intensity and spacing of fringes depends on dynamical scattering  
⇒ can use to measure sample thickness  $t$



# EPFL Bend contours $\iff$ CBED



Bend xtal planes  
with parallel beams

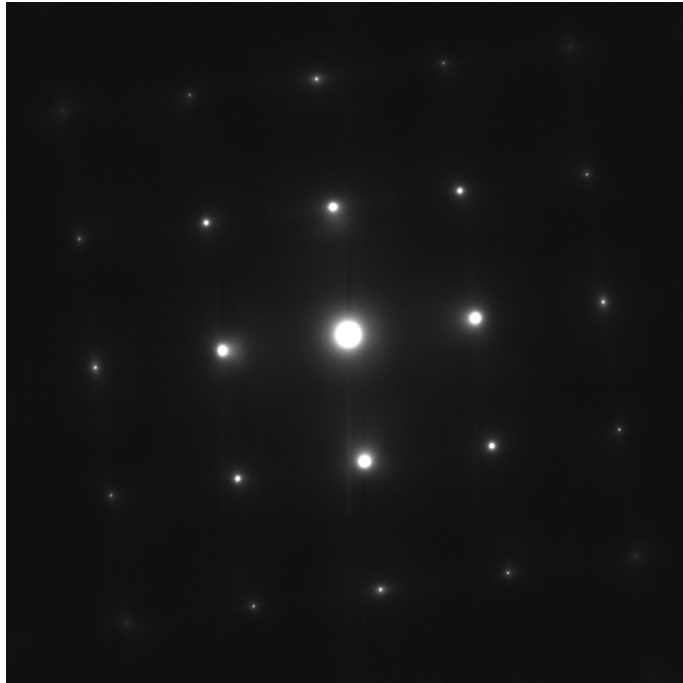


Bend incident beam

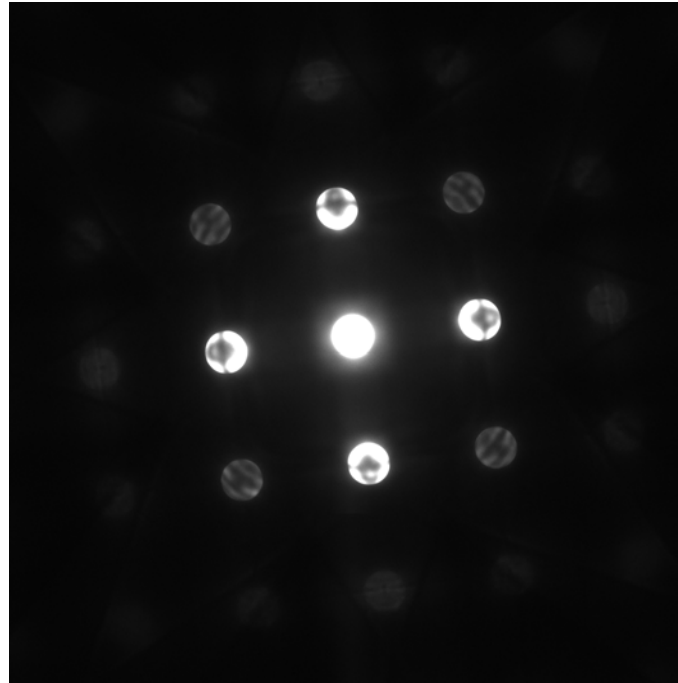
# EPFL Zone axis CBED

- Instead of spot pattern, obtain disc pattern
- Larger convergence semi-angle  $\alpha \Rightarrow$  larger discs

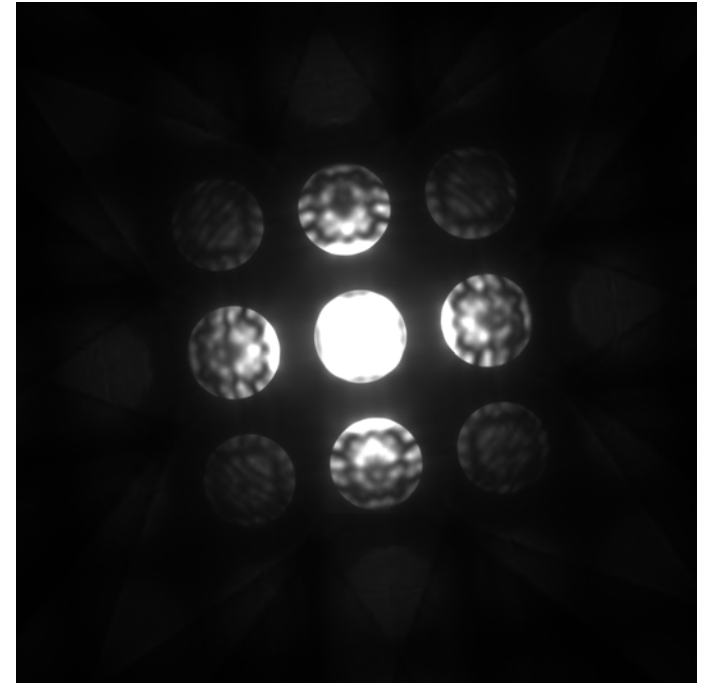
Parallel beam SADP Si [001]



$\alpha \approx 1.6$  mrad



$\alpha \approx 4$  mrad

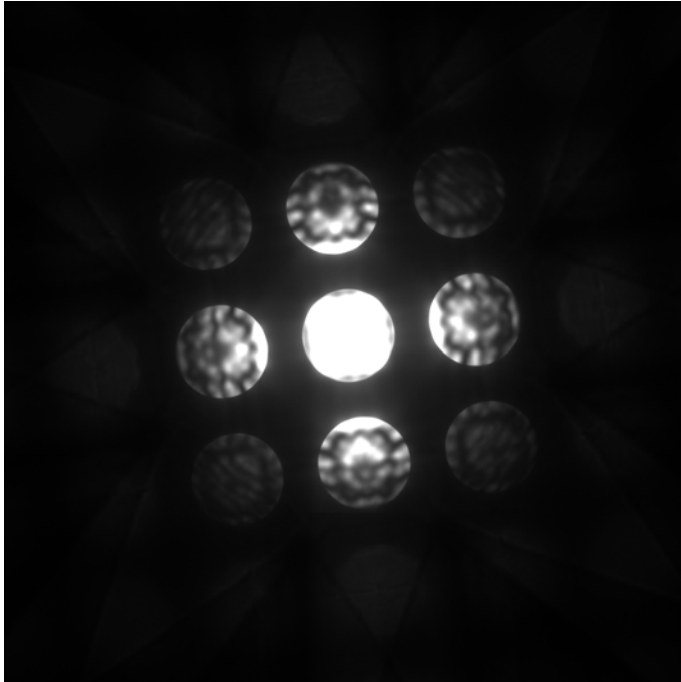


- See complex fringe patterns in discs from dynamical scattering, and symmetry

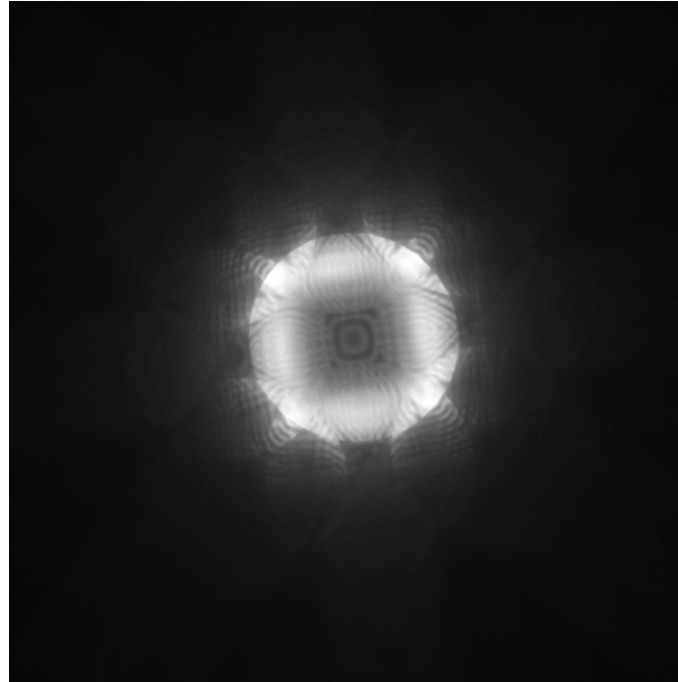
# EPFL Zone axis CBED

- Instead of spot pattern, obtain disc pattern
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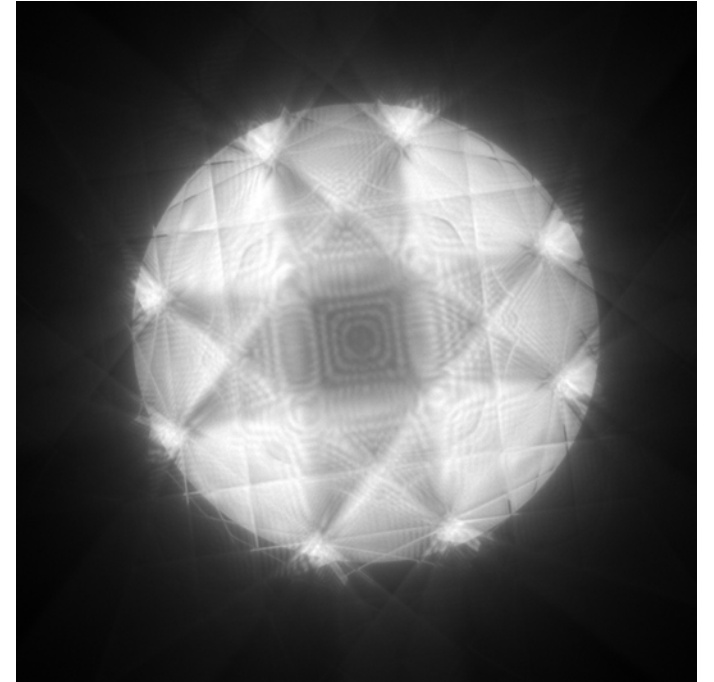
$\alpha \approx 4$  mrad



$\alpha \approx 9$  mrad



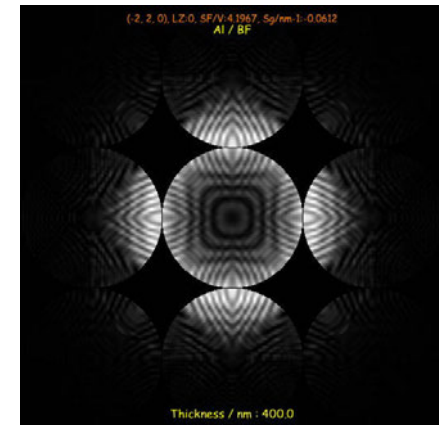
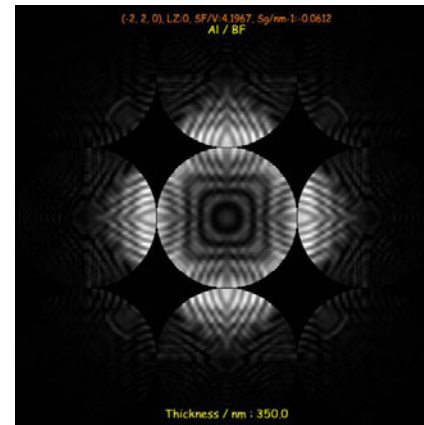
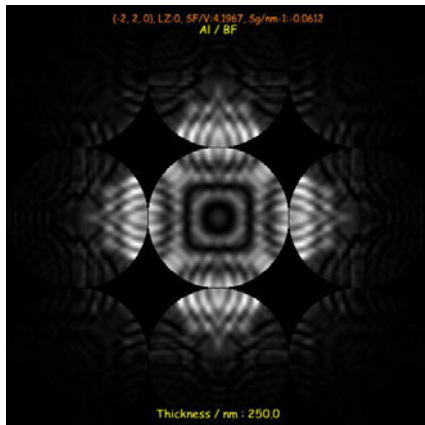
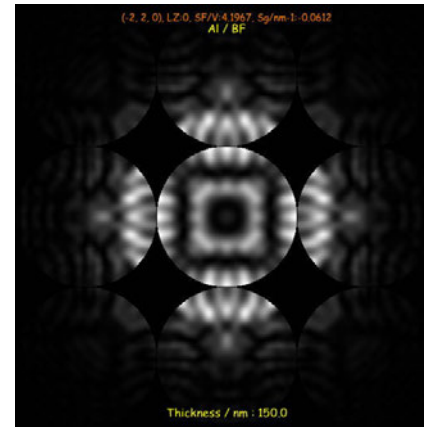
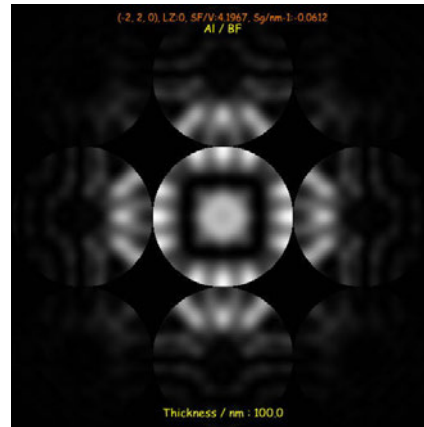
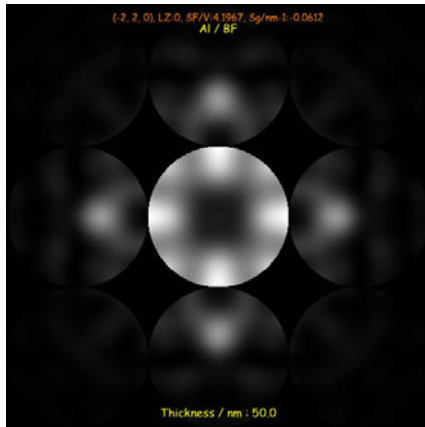
$\alpha \approx 19$  mrad



- See complex fringe patterns in discs from dynamical scattering, and symmetry

# EPFL Zone axis CBED thickness effect

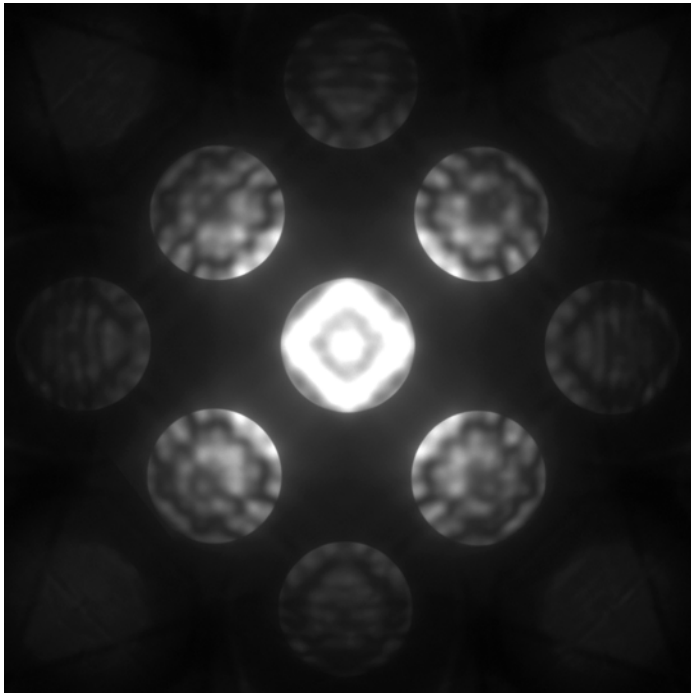
- Measure sample thickness by comparing experimental data to Bloch wave simulations
- Example 1: Bloch wave simulations for Al on  $[0\ 0\ 1]$  zone axis:



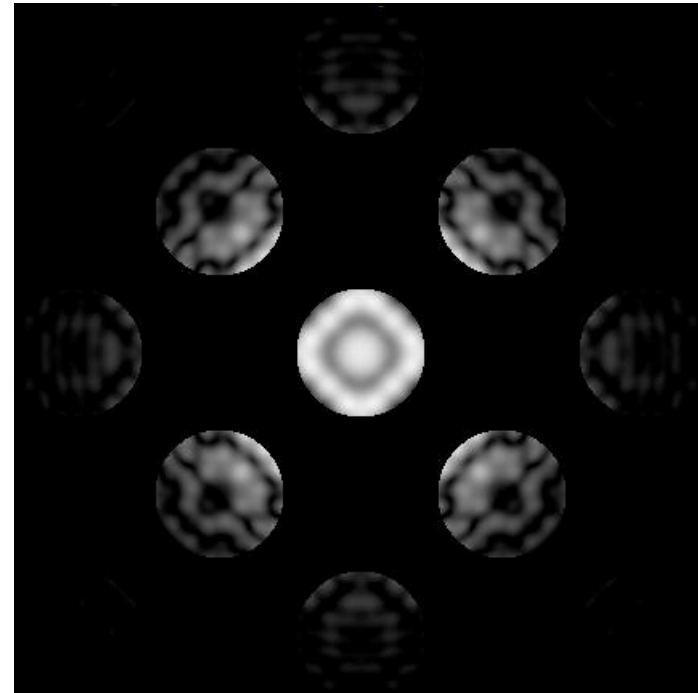


# EPFL Zone axis CBED thickness effect

- Measure sample thickness by comparing experimental data to Bloch wave simulations
- Example 2: experiment vs simulation for Si on [0 0 1] zone axis:



Experiment

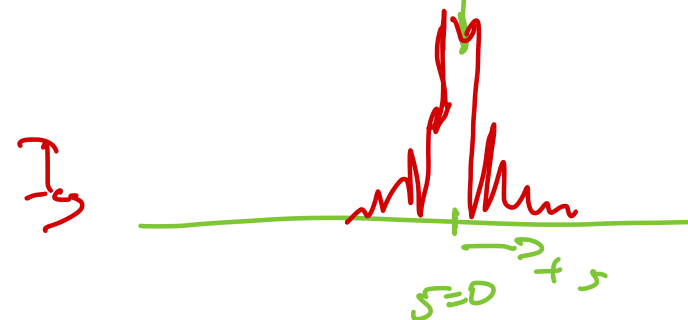
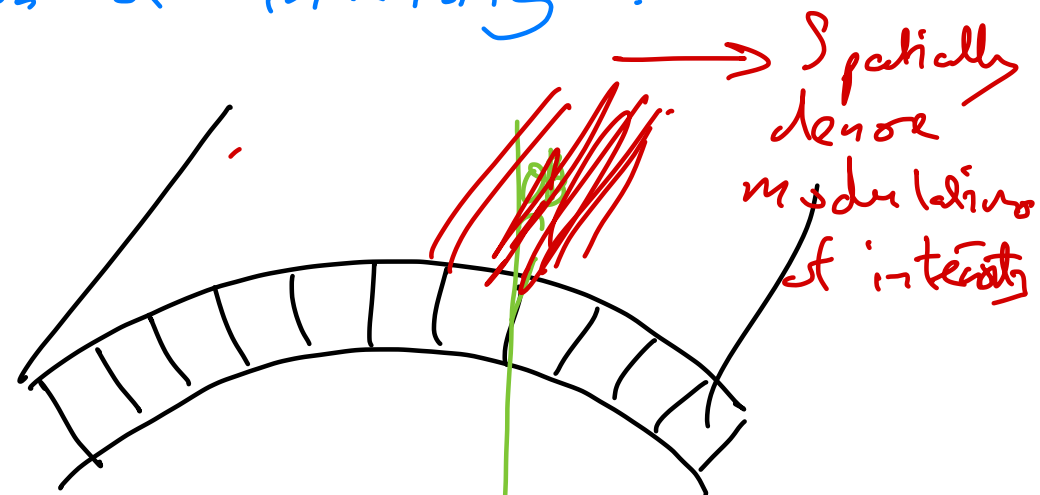
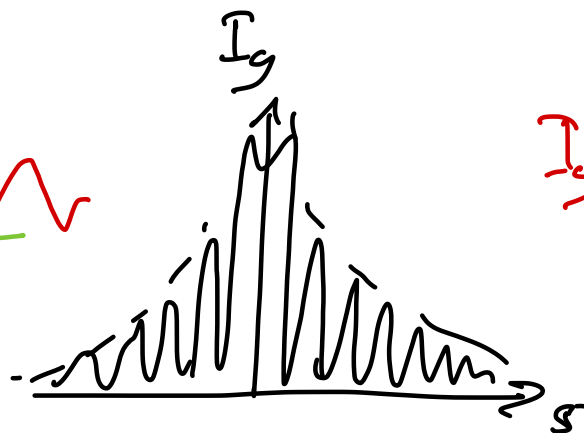
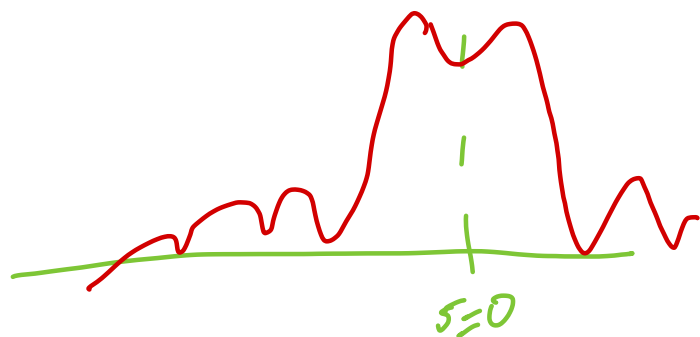
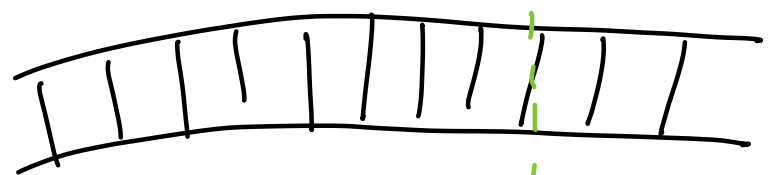


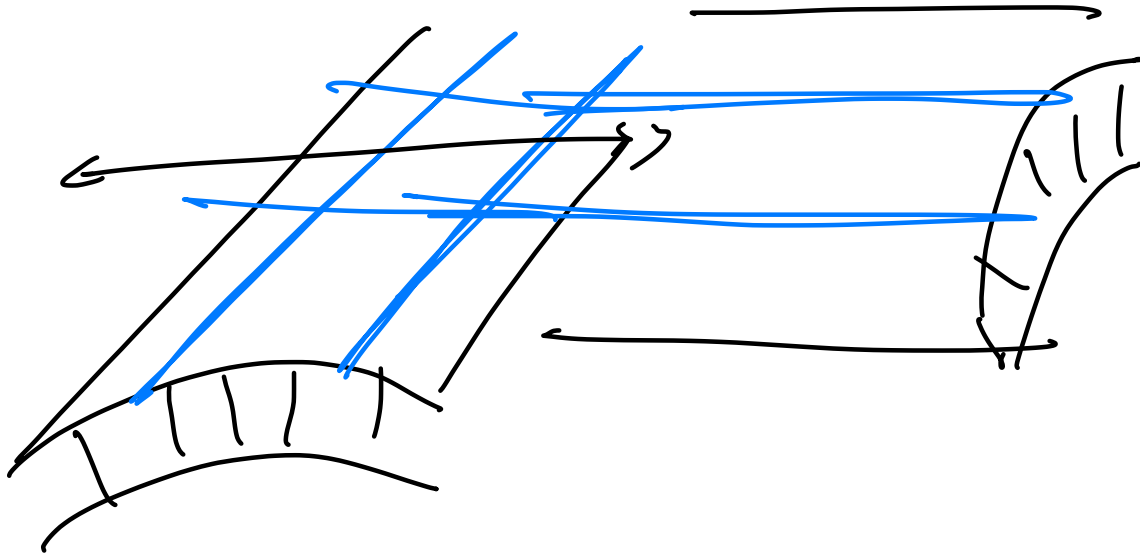
Simulation: 200 kV;  $t = 126\text{nm}$ ;  
 $\alpha = 4.1\text{ mrad}$

- Note: easier to compare to simulations when discs not strongly overlapped



How does local curvature of the crystalline sample influence modulation & intensity?





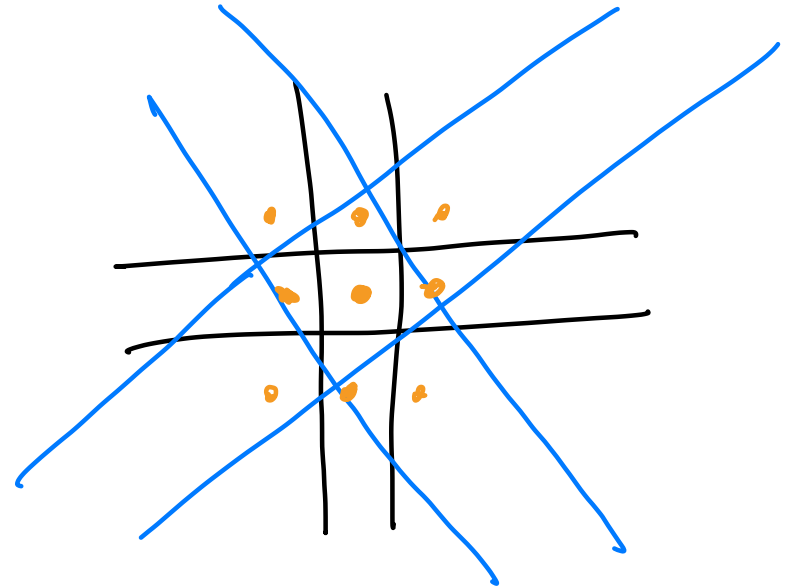
$S_{\text{supp}} \text{ FCC } [001]$

$(200) \rightarrow$

$(020)$

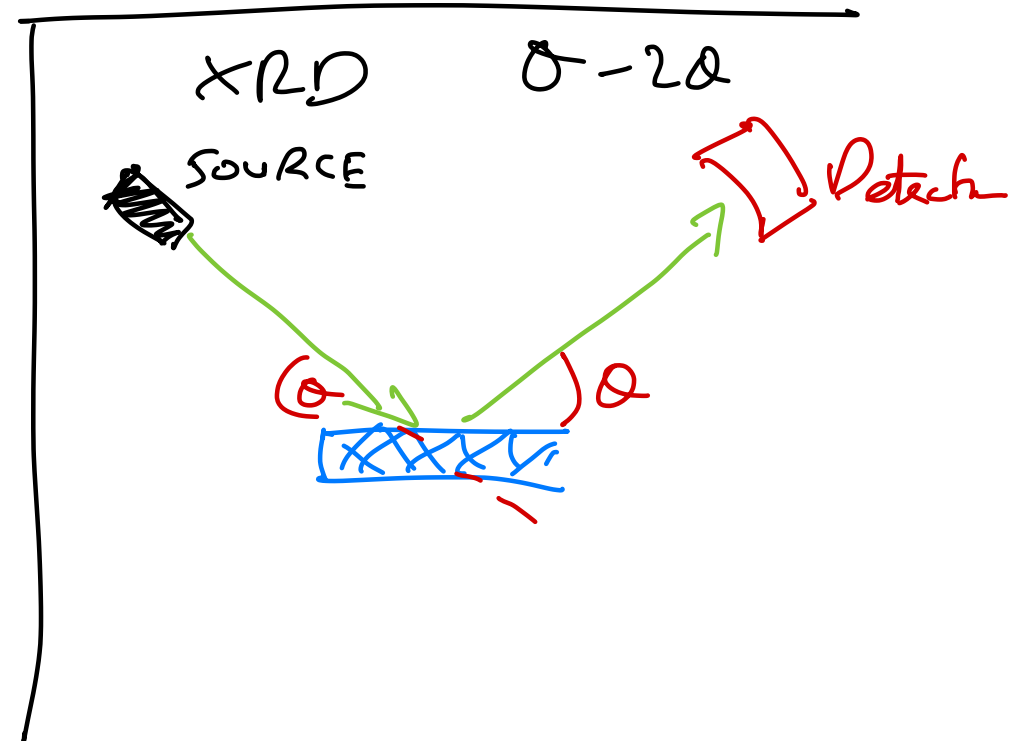
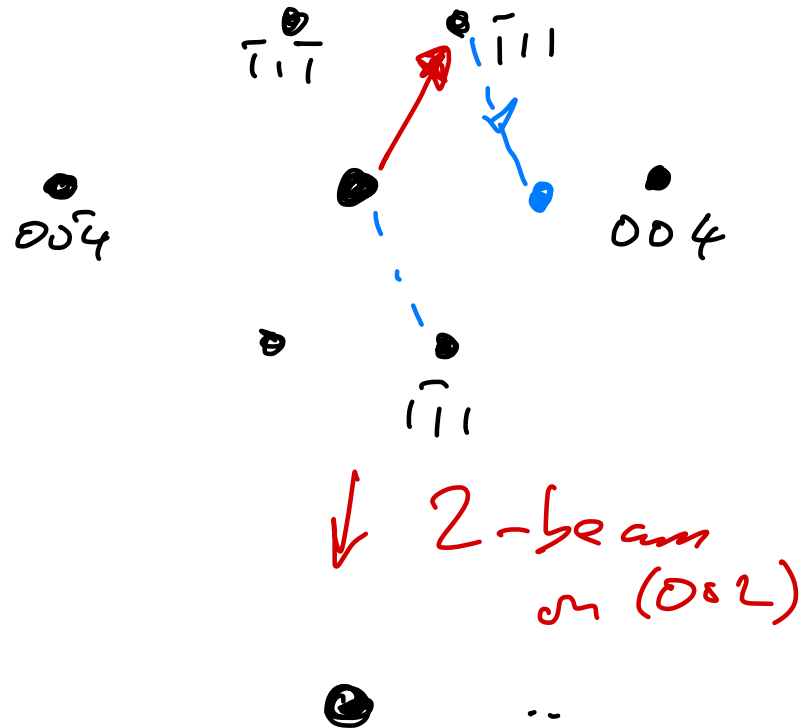
$(220) \cdot$

$(2\bar{2}0) -$



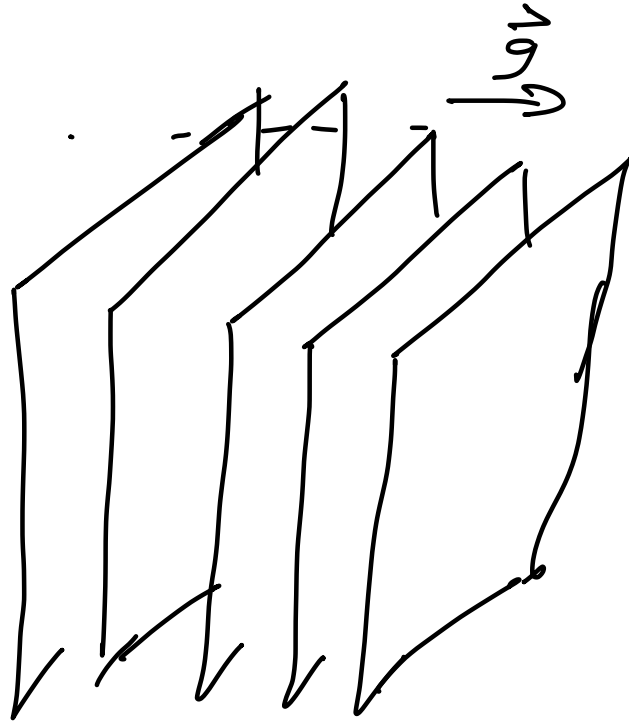
Double diffraction  
 $S: [110]$

$$\bar{1}11 + 1\bar{1}1 = 002$$



Systematic row ?? - Parallel to one set of planes

(200)



SADP:



$$n \lambda \approx 2d_{hkl}$$

$$\Rightarrow \lambda \approx 2d_{nh, nk, nl}$$

Real sample  
Very focused beam samples  
very small and "perfect"  
region

